## New Higher Homework 10

1. $y=x^{3}+x^{2}-16 x-16$.

Find the coordinates of the stationary points and determine their nature.
2. For which values of $x$ is the function $f(x)=\frac{1}{3} x^{3}-2 x^{2}-5 x$ decreasing?
3.


A box with no lid is made by taking a cardboard square of side 10 cm and cutting from its corners four small squares of side $x \mathrm{~cm}$.
(a) Show that the volume is given by $V=4 x^{3}-40 x^{2}+100 x$.
(b) Calculate the maximum possible volume of the box.
4. Find the exact value of each of these logs:
(a) $\quad \log _{3} 27$
(b) $\quad \log _{5} \frac{1}{5}$
5. Simplify
(a) $\quad \log _{6} 9+\log _{6} 4$
(b) $\log _{3} 54-\log _{3} 6$
(c) $3 \log _{2} 16$
6. Solve these equations:
(a) $\quad \log _{2}(x-4)=3$
(b) $4^{t}=33$
7. The sketch shows the graphs of $y=4 x-x^{2}$ and $y=x$.

Calculate the area enclosed by the parabola and the straight line.


